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SECURITY CLASSIFICATION OF THIS PAGE (Blue Data Entered)	
REPORT DOCUMENTATION PAGE	READINSTRUCTIONS EREFORE COMPLETING FORM
1. REPORT NUMBER 2. GOVT ACCESSION OF AD-A091726	O. RESTANDE AUMHER
4. TITLE (and Subilita)	PEOF REPORT & PERIOD COVERED
IMPORTANCE OF PHASE IN SIGNALS	The Control of the Co
•	6. PERFORMING ORG. REPORT NUMBER
7. AUTHOR(a)	8. CONTRACT OR GRANT NUMBER(s)
A.V. Oppenheim and J.S. Lim	N00014-75-C-0951
9. PERFORMING ORGANIZATION NAME AND ADDRESS	10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS
Research Laboratory of Electronics \vee Massachusetts Institute of Technology	NR 049-328
Cambridge, Massachusetts 02139	. KK 013 323
11. CONTROLLING OFFICE NAME AND ADDRESS	12. REPORT DATE
Advanced Research Projects Agency	September 1980
1400 Wilson Boulevard	13. NUMBER OF PAGES
Arlington, VA 22217	8
14. MONITORING AGENCY NAME & ADDRESS(If different from Controlling Office)	15. SECURITY CLASS. (of this report)
Office of Naval Research	Unclassified
Information Systems Program	00240022200

16. DISTRIBUTION STATEMENT (of this Report)

Arlington, VA 22217

Approved for public release; distribution unlimited

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15. DECLASSIFICATION/DOWNGRADING SCHEDULE

17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)

18. SUPPLEMENTARY NOTES

Code 437

Presented at 1980 L'Aquila workshop on Digital Signal Processing, sponsored by IEEE ASSP Society, L'Aquila, Italy, September 1980

19. KEY WORDS (Continue on reverse side if necessary and identify by block number)

ABSTRACT (Continue on reverse side if necessary and identify by block number)

Experimental results supporting the importance of phase

Attempts at explaining the importance of phase

Algorithms for reconstructing a signal from its phase

Potential applications

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IMPORTANCE OF PHASE IN SIGNALS Alan V./Oppenheim Jae S./Lim

Department of Electrical Engineering and Computer Science Research Laboratory of Electronics

Massachusetts Institute of Technology, Cambridge, MA 02139

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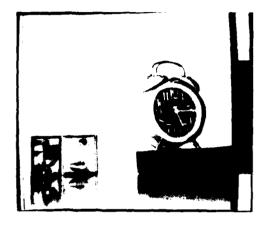
ABSTRACT

- * Experimental results supporting the importance of phase
- * Attempts at explaining the importance of phase
- * Algorithms for reconstructing a signal from its phase
- * Potential applications

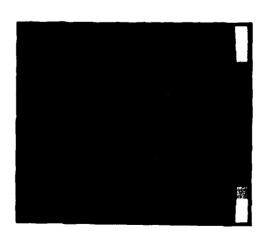
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EXPERIMENTAL RESULTS

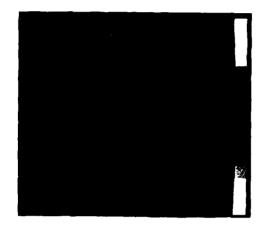
* Fourier synthesis of images



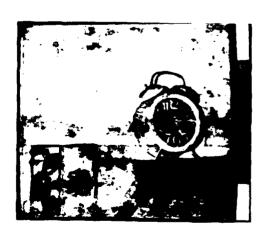
original



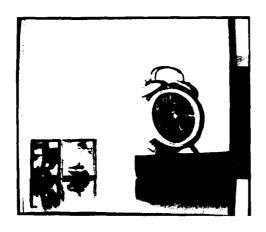
phase: exact
magnitude: unity



phase: zero
magnitude: exact



phase: exact
magnitude: average



original (A)



phase: A
magnitude: B

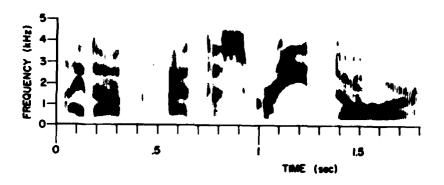


original (B)

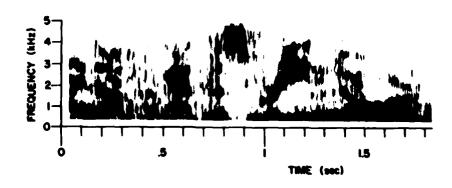


phase: B
magnitude: A

* Fourier synthesis of speech

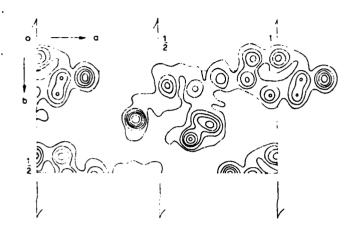


original
(spectrogram of a sentence "Line up at the screen door")

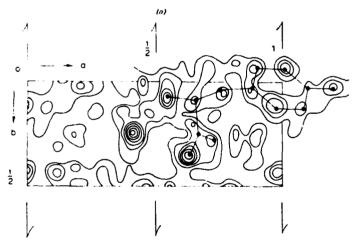


phase: exact
magnitude: unity

* Fourier synthesis of crystallographic structure



original

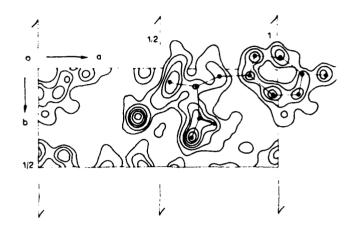


phase: exact

Mary Company

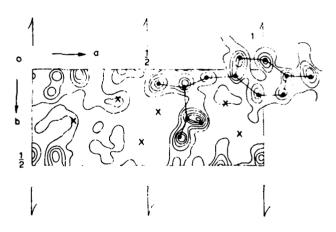
magnitude: random permutation

of exact magnitude



phase: exact

magnitude: tapered constant



phase: exact

magnitude: a different

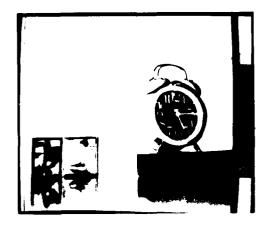
structure

ATTEMPTS AT EXPLAINING IMPORTANCE OF PHASE

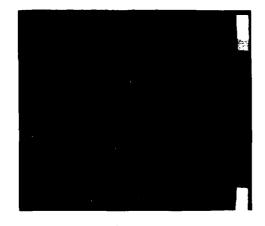
- * For equal RMS error, phase requires two more bits than magnitude (Tescher)
- * Distortion rate theory--For equivalent distortion, phase requires 1.37 bits more than magnitude (Pearlman and Gray)
- * 78% of kinoform (phase-only hologram) represents original image. 22% higher order terms (Kermisch)
- * Relation of correlation of two structures to the correlation of their magnitude-only and phase-only reconstructions: closer for phase-only than magnitude-only (Srinivasan and Chandvasekaran)
- * Event preservation due to zero-phase filtering or edge enhancement due to high-pass filtering (Oppenheim, et.al.)
- * x(n) uniquely specified by N-1 phase samples if
 - (a) x(n) finite duration of length < N and
 - (b) X(z) has no conjugate reciprocal zeros.extendable to 2-D sequences (Hayes, Lim, Oppenheim)

ALGORITHMS FOR SIGNAL RECONSTRUCTION FROM PHASE

* Combining exact phase with unity magnitude

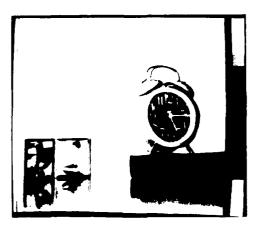


original

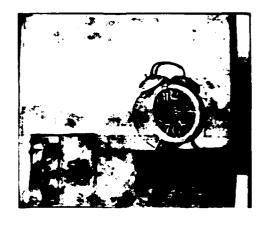


phase: exact
magnitude: unity

* Combining exact phase with average magnitude



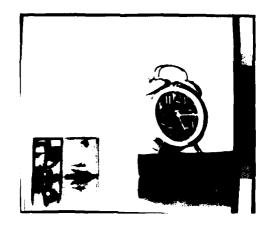
original



phase: exact

magnitude: average

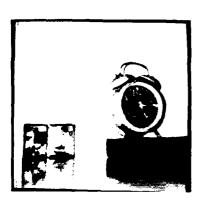
* Combining exact phase with magnitude estimated from degraded magnitude (assumes degraded magnitude is available)



original



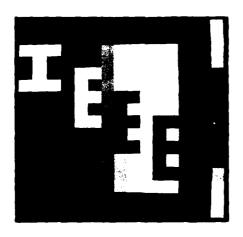
degraded by blurring
with zero-phase blurring function
of short duration



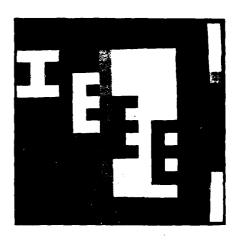
phase: exact

magnitude: estimated

- * Exact reconstruction from phase (assumes the sequence satisfies conditions for unique specification)
 - A. closed form solution definition of phase + a set of N-1 linear equations for a sequence of length N

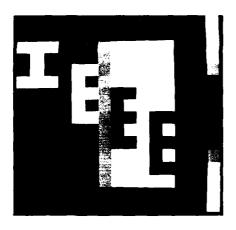


original

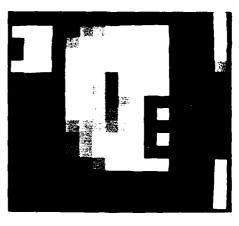


reconstructed

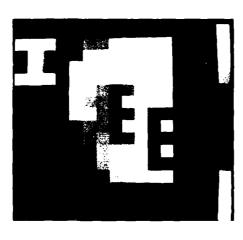
B. Iterative solution
In each iteration, impose known time and frequency
domain constraints (sequence is finite in duration
and is constrained by known phase samples)



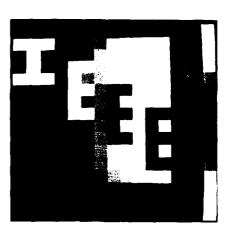
original



result after 10 iterations



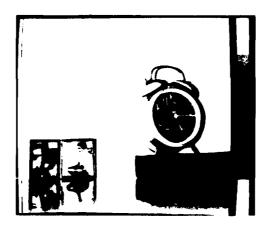
result after 50 iterations



result after 400 iterations

POTENTIAL APPLICATIONS

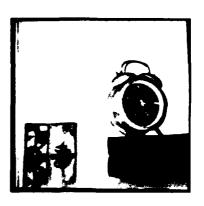
* Blind deconvolution



original



zero phase blurring



restored

- * Fourier transform signal coding

 Code only phase and reconstruct the signal from only its phase.
- * Improvement of computer generated holograms
- * Signal registration
- * Signal restoration

 Importance of phase emphasizes importance of accurate estimation of phase in signal restoration

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